

# ASSOCIATIVE SELF-ORGANIZING MAP

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**Abstract:** We present a study of a novel variant of the Self-Organizing Map (SOM) called the Associative Self-Organizing Map (A-SOM). The A-SOM is similar to the SOM and thus develops a representation of its input space, but in addition it also learns to associate its activity with the activity of one or several external SOMs. The A-SOM has relevance in e.g. the modelling of expectations in one modality due to the activity invoked in another modality, and in the modelling of the neuroscientific simulation hypothesis. The paper presents the algorithm generalized to an arbitrary number of associated activities together with simulation results to find out about its performance and its ability to generalize to new inputs that it has not been trained on. The simulation results were very encouraging and confirmed the ability of the A-SOM to learn to associate the representations of its input space with the representations of the input spaces developed in two connected SOMs. Good generalization ability was also demonstrated.

## 1 INTRODUCTION

A dramatic illustration of the interaction of different modalities can be seen in the McGurk-MacDonald effect. If you hear a person making the sound /ba/ but the sound is superimposed on a video recording on which you do not see the lips closing, you may hear the sound /da/ instead (McGurk and MacDonald, 1976). The neural mechanisms underlying such interaction between different sensory modalities are not known but recent evidence suggests that different primary sensory cortical areas can influence each other. Another familiar example is that the sensory information gained when the texture of an object is felt in the pocket can invoke visual images/expectations of the object.

An efficient multimodal perceptual system should be able to associate different modalities with each other in this way. This provides an ability to activate the subsystem for a modality even when its sensory input is limited or nonexistent as long as there are activities in subsystems for other modalities, which the subsystem has learned to associate with certain patterns of activity, which usually comes together with the patterns of activity in the other subsystems.

This paper explores a novel variant of the Self-Organizing Map (SOM) (Kohonen, 1988) called the Associative Self-Organizing Map (A-SOM). The A-SOM differs from earlier attempts to build associative maps such as the Adaptive Resonance Associative Map (Tan, 1995) and Fusion ART (Nguyen et al., 2008) in that all layers (or individual networks) share the same structure and uses topologically arranged representations. Unlike ARTMAP, the A-SOM also allows associations to be formed in both directions (Carpenter et al., 1992). The A-SOM is an extension to the SOM, which learns to associate its activity with the activities of other SOMs. Previously versions of the A-SOM has been restricted to association with only one SOM (Johnsson and Balkenius, 2008). This work was done in the context of haptic perception where a bio-inspired self-organizing texture and hardness perception system automatically learned to associate the representations of two submodalities (A-SOMs) with each other. The system employed a microphone based texture sensor and a hardness sensor that measured the compression of the explored material while applying a constant pressure. It successfully found associated representations of the texture and hardness submodalities when trained and tested

with multiple samples gained from the exploration of a set of 4 soft and 4 hard objects of different materials with varying surface textures. However the version of the A-SOM used in this context was only able to associate with one SOM and its generalization ability was not explored at all.

The A-SOM explored in this paper has been generalized to enable association with an arbitrary number of SOMs. We have tested the generalized A-SOM with training and test sets constructed by selecting uniformly distributed random points from a subset of the plane, while employing Voronoi tessellations of this plane as well as of the grid of neurons constituting the A-SOM to determine its performance. The implementation was done in C++ using the neural modeling framework Ikaros (Balkenius et al., 2008).

## 2 A-SOM

The A-SOM (Fig. 1) can be considered as a SOM which learns to associate its activity with additional ancillary inputs from a number of additional SOMs. It consists of an  $I \times J$  grid of neurons with a fixed number of neurons and a fixed topology. Each neuron  $n_{ij}$  is associated with  $r + 1$  weight vectors, where  $w_{ij}^a \in R^n$  is used for the main input and  $w_{ij}^1 \in R^{m_1}, w_{ij}^2 \in R^{m_2}, \dots, w_{ij}^r \in R^{m_r}$  are used for the ancillary inputs. All the elements of all the weight vectors are initialized by real numbers randomly selected from a uniform distribution between 0 and 1, after which all the weight vectors are normalized. At time  $t$  each neuron  $n_{ij}$  receives  $r + 1$  input vectors  $x^a(t) \in R^n$  and  $x^1(t) \in R^{m_1}, x^2(t) \in R^{m_2}, \dots, x^r(t) \in R^{m_r}$ .

The main net input  $s_{ij}$  is calculated using the standard cosine measurement

$$s_{ij}(t) = \frac{x^a(t)w_{ij}^a(t)}{|x^a(t)||w_{ij}^a(t)|}, \quad (1)$$

The activity in the neuron  $n_{ij}$  is given by

$$y_{ij}(t) = [y_{ij}^a(t) + y_{ij}^1(t) + y_{ij}^2(t) + \dots + y_{ij}^r(t)] / (r + 1) \quad (2)$$

where the main activity  $y_{ij}^a$  is calculated using the softmax function (Bishop, 1995)

$$y_{ij}^a(t) = \frac{(s_{ij}(t))^m}{\arg \max_k (s_k(t))^m} \quad (3)$$

where  $k$  ranges over the neurons in the neural network and  $m$  is the softmax exponent. Like the main activity, the ancillary activity  $y_{ij}^p(t)$ ,  $p = 1, 2, \dots, r$  is

calculated by using the standard cosine measurement between the ancillary inputs and the corresponding weights.

$$y_{ij}^p(t) = \frac{x^p(t)w_{ij}^p(t)}{|x^p(t)||w_{ij}^p(t)|}. \quad (4)$$

The neuron  $c$  associated with the weight vector  $w_c^a(t)$  most similar to the input vector  $x^a(t)$ , i.e. the neuron with the strongest main activation, is selected:

$$c = \arg \max_c \{ |x^a(t)w_c^a(t)| \} \quad (5)$$

The weights for the main input  $w_{ijk}^a$  are subsequently adapted by

$$w_{ijk}^a(t + 1) = w_{ijk}^a(t) + \alpha(t)G_{ijc}(t) \left[ x_k^a(t) - w_{ijk}^a(t) \right] \quad (6)$$

where  $0 \leq \alpha(t) \leq 1$  is the adaptation strength with  $\alpha(t) \rightarrow 0$  when  $t \rightarrow \infty$  and the neighbourhood function  $G_{ijc}(t)$  is a Gaussian function decreasing with time.

The weights  $w_{ijl}^p, p = 1, 2, \dots, r$ , for the ancillary inputs are adapted by

$$w_{ijl}^p(t + 1) = w_{ijl}^p(t) + \beta x_l^p(t) \left[ y_{ij}^a(t) - y_{ij}^p(t) \right] \quad (7)$$

where  $\beta$  is the constant adaptation strength. All weights  $w_{ijk}^a(t)$  and  $w_{ijl}^p(t)$  are normalized after each adaptation.

## 3 EXPERIMENTS AND RESULTS

### 3.1 Associating the A-SOM with Two Ancillary SOMs

We have evaluated the A-SOM by setting up a system consisting of one A-SOM and two connected SOMs (Fig. 2). To this end a set containing 10 training samples were constructed. This was done by randomly generating 10 points with a uniform distribution from a subset  $s$  of the plane  $s = \{(x, y) \in R^2; 0 \leq x \leq 1, 0 \leq y \leq 1\}$  (Fig. 3, left). The selected points were then mapped to a subset of  $R^3$  by adding a third constant element of 0.5, yielding a training set of three-dimensional vectors. The reason for this was that a Voronoi tessellation of the plane was calculated from the generated points to later aid in the determination of where new points in the plane were expected to invoke activity in the A-SOM. To make this Voronoi tessellation, which is based on a Euclidian metric,

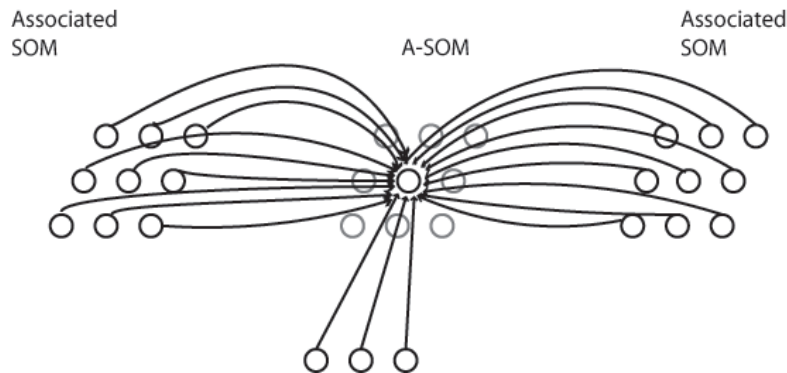


Figure 1: The connectivity of the A-SOM neural network. During training each neuron in an A-SOM receives two kinds of input. One kind of input is the main (bottom-up) input, which corresponds to the input an ordinary SOM receives. The other kind of input is the activity of each neuron in one or more associated ancillary SOMs. In the fully trained A-SOM, activity can be triggered by either main input or by activity in one or several of the ancillary SOMs, or both.

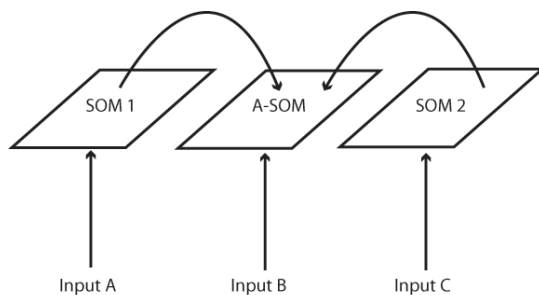


Figure 2: Schematic depiction over the connections between the two SOMs and the A-SOM in the architecture of the test system used for this paper. The test system consist of three subsystems, which develop representations of sample sets from three input spaces (for simplicity we use the same input set for all three representations in the study for this paper). One of the representations (the A-SOM) also learns to associate its activity with the simultaneous activities of the two SOMs. This means proper activity can be invoked in the A-SOM of the fully trained system even if it does not receive any ordinary input. This is similar to cross-modal activation in humans, e.g. a tactile perception of an object can invoke an internal visual imagination of the same object.

useful for this purpose with the A-SOM, which uses a metric based on dot product, the set of points in the plane has to be mapped so that the corresponding position vectors after normalization are unique. One way to accomplish such a mapping is by adding a constant element to each vector. The result of this is that each vector will have a unique angle in  $R^3$ . We chose the value 0.5 for the constant elements to maximize the variance of the angles in  $R^3$ .

The A-SOM was connected to two SOMs (using the same kind of activation as the main activation in the A-SOM, i.e. dot product with softmax activation) called SOM 1 and SOM 2, and thus also receive their

respective activities as associative input, see Fig. 2. The A-SOM, SOM 1 and SOM 2 were then simultaneously fed with samples from the training set, during a training phase consisting of 20000 iterations. The two SOMs and the A-SOM could as well be fed by samples from three different sets, always receiving the same combinations of samples from the three sets (otherwise the system could not learn to associate them). This could be seen as a way of simulating simultaneous input from three different sensory modalities when an animal or a robot explores a particular object. Each of the three representations, the A-SOM and the two SOMs, consists of  $15 \times 15$  neurons. The softmax exponent for each of them were set to 1000. Their learning rate  $\alpha(0)$  was initialized to 0.1 with a learning rate decay of 0.9999 (i.e. multiplication of the learning rate with 0.9999 in each iteration), which means the minimum learning rate, set to 0.01, will be reached at the end of the 20000 training iterations. The neighbourhood radius, i.e. the sigma of the neighbourhood function, was initialized to 15 for all three representations and shrunk to 1 during the 20000 training iterations by using a neighbourhood decay of 0.9998 (i.e. multiplication of the neighbourhood radius with 0.9998 in each iteration). All three representations used plane topology when calculating the neighbourhood. The  $\beta$  for the associative weights in the A-SOM was set to 0.35.

After training the system was evaluated by feeding it with samples from the training set again to one, two or all three representations in all possible combinations. When a representation did not receive any input it was fed with null vectors instead (thus simulating the input of no signal from sensors of the modality of that representation). The centers of activity in the A-SOM as well as in the two SOMs were recorded for

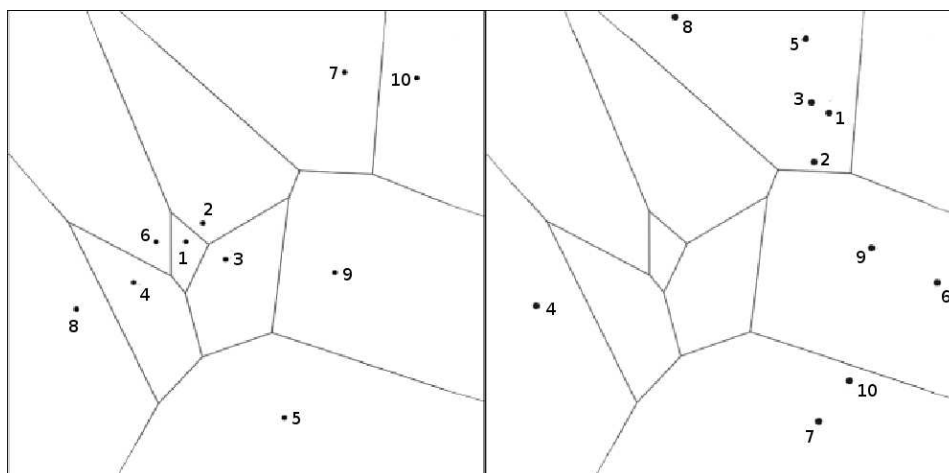


Figure 3: Left: The Voronoi tessellation of the points used when constructing the training set used for the A-SOM and the two SOMs. This set was constructed by randomly generating 10 points from a subset of  $R^2$  according to a uniform distribution. To make this Voronoi tessellation, which is based on a Euclidian metric, valid as a measure of proximity the training set had to be transformed by addition of a constant element to each sample vector. This is because the A-SOM using a dot product based metric and normalizing its input would consider all position vectors of a particular angle equal. By adding a constant element each point in the plane becomes a position vector in  $R^3$  with a unique angle. Right: The same Voronoi tessellation but with the points used in the generalization test depicted. Also this set was mapped to a new set in  $R^3$  by addition of a third constant element to each sample vector, and for the same reason as for the samples in the training set.

all these tests.

The result was evaluated by using the training set on the fully trained system. First we recorded the centers of activation in the A-SOM when fed by main input from the training set only (i.e. the two SOMs were fed with null vectors) and the centers of activation in the two SOMs. Then we calculated Voronoi tessellations for the centers of activation in all three representations (Fig. 4, uppermost row) to see if they could separate the samples and in particular if the A-SOM could separate the samples when fed by the activity of one or both of the SOMs only. If the center of activation for a particular sample in the training set were located in the correct Voronoi cell, this is considered as a successful recognition of the sample, because this means the center of activation is closer to the center of activation of the same object than to the center of activation of any other sample in the training set when the A-SOM is fed by main input only like an ordinary SOM. By comparing the Voronoi tessellations of the A-SOM and the two SOMs (Fig. 4) and the Voronoi tessellation of the plane for the training set (Fig. 3) we can see that the ordering of the Voronoi cells for the training set are to a large extent preserved for the Voronoi cells for the centers of activation in the A-SOM and the two SOMs. In Fig. 4 we can also see that all, i.e. 100% of the training samples are recognized in the A-SOM as long as at least one of the three representations received input.

### 3.2 Generalization

To test if the system was able to generalize to a new set of samples, which it had not been trained with, we constructed a new set of 10 samples with the same method as for the training set. This generalization test set was used as input to the two SOMs and the A-SOM, i.e. each of these representations received the same sample simultaneously (or a null vector).

The generalization ability of the system was evaluated by feeding it with samples from the generalization set to one, two or all three representations in all possible combinations. When a representation did not receive any input it was fed with null vectors instead. The centers of activity in the A-SOM as well as in the two SOMs were recorded for all these tests.

The result was evaluated by now using the generalization set on the fully trained system. We recorded the centers of activation in the A-SOM when each of the SOMs were the only recipient of input, when both SOMs received input, when each of the SOMs and the A-SOM received input, when all three representations received input, and when only the A-SOM received input. As before a representation which did not receive input received null vectors (signifying the lack of sensory registration for that modality). We then looked at in which Voronoi cell the centre of activation was located in the A-SOM and in the SOMs for each sample of the generalization set. When a gener-

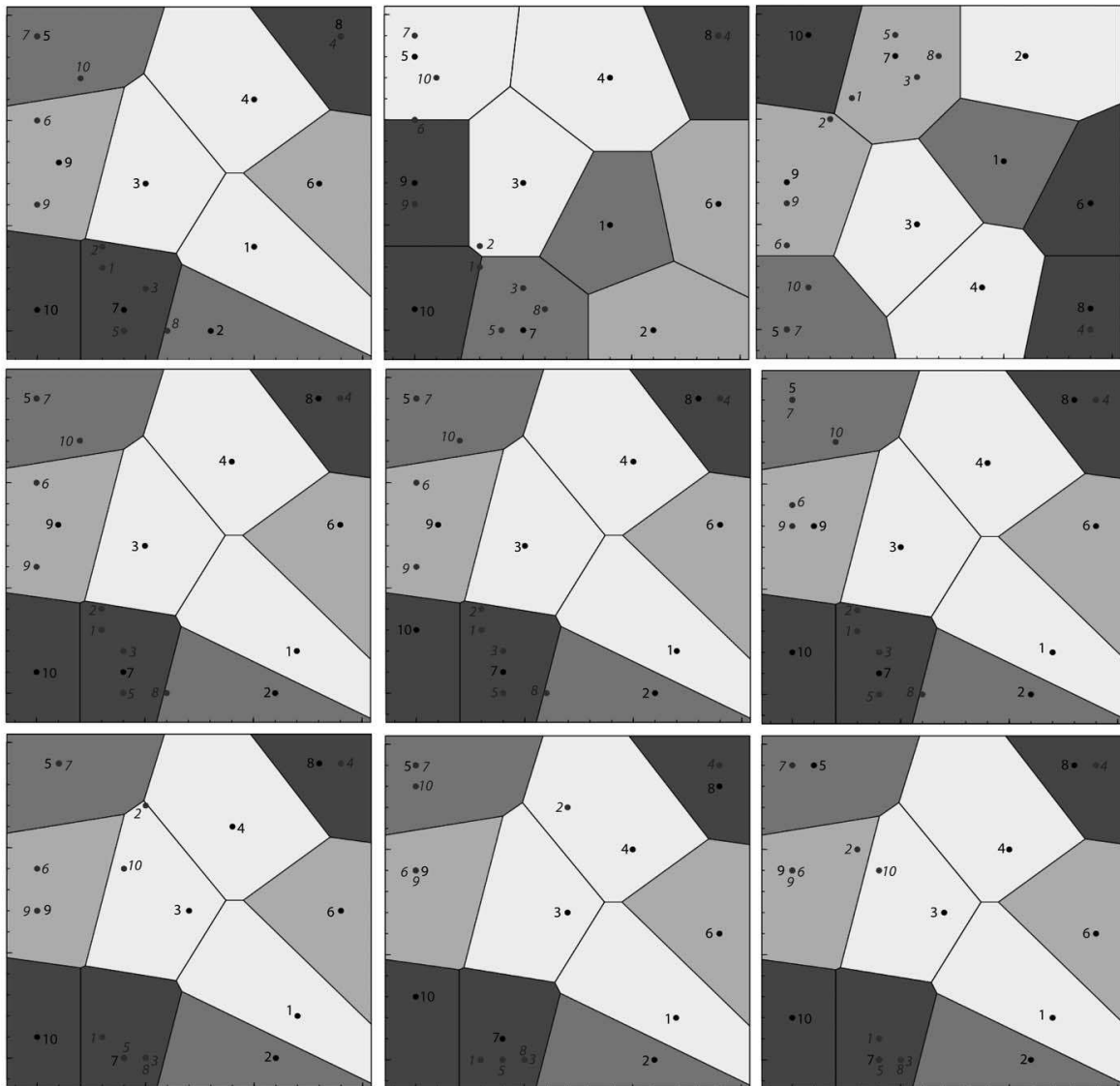


Figure 4: The center of activation for different constellations of input to the fully trained system in the A-SOM and in the two SOMs. The centers of activation for the training samples and the generalization samples are denoted by numbers with normal and italic typefaces respectively. Upper row left: The A-SOM when only main input to the A-SOM is received. The Voronoi tessellation for these centers of activation has also been drawn. This is also true for the other images in this figure depicting activations in the A-SOM. Upper row middle: The SOM1 with the Voronoi tessellation for the training set drawn. Upper row right: The SOM2 with the Voronoi tessellation for the training set drawn. Middle row left: The A-SOM receiving main input and the activity of SOM1. Middle row middle: The A-SOM when receiving main input and the activity of SOM2. Middle row right: The A-SOM when receiving main input and the activities of SOM1 and SOM2. Lower row left: The A-SOM when receiving the activity of SOM1 only. Lower row middle: The A-SOM when receiving the activity of SOM2 only. Lower row right: The A-SOM receiving the activities of SOM1 and SOM2.

alization sample belongs to the Voronoi cell for sample  $k, k = 1, 2, \dots, 10$  of the training set (see Fig. 3) and its activation in the A-SOM or one of the SOMs is located in the Voronoi cell for the centre of activation for the same training sample (see Fig. 4), then we consider the centre of activation for the generalization sample to be properly located and we consider it to be

successfully generalized.

Leftmost in the upper row of Fig. 4 we can see that the centers of activation for all the generalization samples besides sample 8 is within the correct Voronoi cell in the A-SOM when it receives main input only. However that sample 8 is outside, and barely so, the correct Voronoi cell is probably not an indica-

tion that it is incorrect because the A-SOM consists of 225 neurons and is not a continuous surface but a discretized representation.

In the middle of the upper row of Fig. 4 we can see that all centers of activation for the generalization samples are correctly located in SOM1 besides 1 and 6 which are on the border to the correct Voronoi cell (but this should probably not be considered an indication of incorrectness for the same reason as mentioned above), and 2 which is located close to the correct Voronoi cell.

Rightmost of the upper row of Fig. 4 we can see that all centers of activation for the generalization samples are correctly located in SOM2 besides 2, which is located close to the correct Voronoi cell.

Leftmost in the middle row of Fig. 4 we can see that the centers of activation for all the generalization samples besides sample 8 (which should probably not be considered an indication of incorrectness for the same reason as mentioned above) is within the correct Voronoi cell in the A-SOM when it receives main input as well as the activity of SOM1 as input.

In the middle of the middle row of Fig. 4 we can see that the centers of activation for all the generalization samples besides sample 8 (which should probably not be considered an indication of incorrectness for the same reason as mentioned above) is within the correct Voronoi cell in the A-SOM when it receives main input as well as the activity of SOM2 as input.

Rightmost of the middle row of Fig. 4 we can see that the centers of activation for all the generalization samples besides sample 8 (which should probably not be considered an indication of incorrectness for the same reason as mentioned above) is within the correct Voronoi cell in the A-SOM when it receives main input as well as the activities of both SOM1 and SOM2 as input.

Leftmost of the lower row of Fig. 4 we can see that the centers of activation for all the generalization samples besides sample 2 and 10, i.e. 80%, is within the correct Voronoi cell in the A-SOM when it receives the activity of SOM1 as its only input.

In the middle of the lower row of Fig. 4 we can see that the centers of activation for all the generalization samples besides sample 2, i.e. 90%, is within the correct Voronoi cell in the A-SOM when it receives the activity of SOM2 as its only input.

Rightmost of the lower row of Fig. 4 we can see that the centers of activation for all the generalization samples besides sample 2 and 10, i.e. 80%, is within the correct Voronoi cell in the A-SOM when it receives the activities of SOM1 and SOM2 as its only input.

In Fig. 5 we can see a graphical representation of

the activity in the two SOMs as well as total, main and ancillary activities of the A-SOM while receiving a sample from the generalization set. The lighter an area is in this depiction, the higher the activity is in that area.

## 4 DISCUSSION

We have presented and experimented with a novel variant of the Self-Organizing Map (SOM) called the Associative Self-Organizing Map (A-SOM), which develops a representation of its input space but also learns to associate its activity with the activities of an arbitrary number of ancillary SOMs. In our experiments we connected an A-SOM to two ancillary SOMs and all these were trained and tested with a set of random samples of points from a subset of the plane. In addition we tested the generalization ability of the system by another set of random points generated from the same subset of the plane. The algorithm was generalized to enable association with an arbitrary number of ancillary SOMs. Moreover this study have also tested the ability of an A-SOM based system to generalize its learning to new samples. The ability of the A-SOM proved to be good, with 100% accuracy with the training set and about 80-90% accuracy in the generalization tests, depending on which constellation of inputs which was provided to the system. It was also observed that the generalization in the ordinary SOMs was not perfect. If this had been perfect the generalization ability would probably be even better. This is probably a matter of optimizing the parameter settings.

In this experiment we connected an A-SOM with two SOMs, but we can see no reasons to why it should not be possible to connect an arbitrary numbers of A-SOMs to each other. Johnsson and Balkenius successfully connected two A-SOMs with each other in the context of a hardness/texture sensing system (Johnsson and Balkenius, 2008). In the present study we used the same training set and the same generalization set as input for the A-SOM and for each of the two SOMs. This was for simplicity reasons and in particular because it made it easier to present the results and to relate the organizations of the SOMs and the A-SOM to each other.

It is interesting to speculate, and later test, whether there are any restrictions on the sets that are used as input to the different SOMs and A-SOMs in this kind of system. A reasonable guess would be that to learn to associate the activity arising from the training sets impose no restrictions on the training sets, but when it comes to generalization there would probably be one

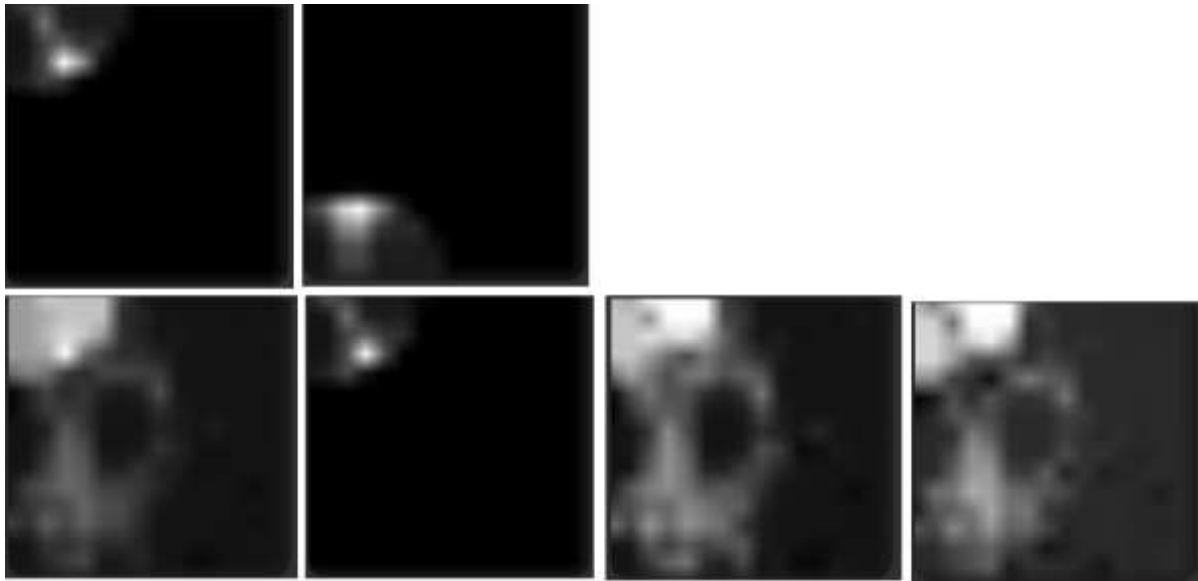


Figure 5: Activations at a moment in the simulation. The lighter an area is in this depiction, the higher the activity is in that area. Upper row left: The activity in SOM1. Upper row right: The activity in SOM2. Lower row left: The total activity in the A-SOM. Lower row, the second image from the left: The main activity in the A-SOM. Lower row, the third image from the left: The ancillary activity in the A-SOM due to the activity in SOM1. Lower row right: The ancillary activity in the A-SOM due to the activity in SOM2.

restriction. The restriction is that there should probably need to exist a topological function between the different input spaces so that the sequences of input samples from the different input spaces will invoke traces of activities over time in their respective SOM or A-SOM that in principle would be possible to map on each other by using only translations, rotations, stretching and twisting. Otherwise the generalization would be mixed up at least partially. The same would be true if the parameter setting implies the development of fragmented representations.

Our system can be seen as a model of a neural system with two monomodal representations (the two SOMs) and one multimodal representation (the A-SOM) constituting a neural area that merges three sensory modalities into one representation.

The A-SOM actually develops several representations, namely one representation for its main input (the main activity) and one representation for each of the ancillary SOMs it is connected to (the ancillary activities), and one representation which merges these individual representations (the total activity). One could speculate whether something similar could be found in cortex, perhaps these different representations could correspond to different cortical layers.

Interaction between sensory modalities may also be important for perceptual simulation. An idea that has been gaining popularity in cognitive science in recent years is that higher organisms are capable of

simulating perception. In essence, this means that the perceptual processes normally elicited by some ancillary input can be mimicked by the brain (Hesslow, 2002). There is now a large body of evidence supporting this contention. For instance, several neuroimaging experiments have demonstrated that activity in visual cortex when a subject imagines a visual stimulus resembles the activity elicited by a corresponding ancillary stimulus (for a review of this evidence see e.g. (Kosslyn et al., 2001); for a somewhat different interpretation, see (Bartolomeo, 2002).

A critical question here is how simulated perceptual activity might be elicited. One possibility is that signals arising in the frontal lobe in anticipation of consequences of incipient actions are sent back to sensory areas (Hesslow, 2002). Another possibility is that perceptual activity in one sensory area can influence activity in another. The A-SOM provides a mechanism whereby sensory activity in an artificial system might be elicited or modulated by activity in a different sensory modality.

It should be noted that the model presented here is consistent with different views of how the sensory system is organized. The traditional view of sensory information processing has been that of a hierarchically organized system. Unimodal neurons in primary sensory cortex send signals to higher association areas where information from different modalities are eventually merged. The model presented in this pa-

per is consistent with such a view. The A-SOM in fig. 2 could be seen as being a step higher in the sensory hierarchy than SOM-1 and SOM-2 and could project to other A-SOMs further up the hierarchy. However, recent neuroscientific evidence suggests that different primary sensory cortical areas can influence each other more directly. For instance, in a recent fMRI study (Kayser et al., 2007) recently showed that visual stimuli can influence activity in primary auditory cortex. The associative SOM can serve as a model of such an organization as well. As an illustration, SOM-1 and A-SOM in fig. 2 could be located in an analog of a primary sensory cortical area, say an auditory area, and be influenced by signals from SOM-2, which could be located in a different, say visual, area.

In the future we will try to extend the ideas presented in this paper to beside sensory neural networks also include motor neural networks. In this way we hope to be able to explore the neuroscientific simulation hypothesis (Hesslow, 2002).

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